

# Autopilot Design for an Unmanned Surface Vehicle Based on Backstepping Integral Technique with Experimental Results

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## Abstract

Controller tuning is the correct setting of controller parameters to control complex dynamic systems appropriately and with high accuracy. Therefore, this study addressed the development of a method for tuning the heading controller of an unmanned surface vehicle (USV) based on the backstepping integral technique to enhance the vehicle behavior while tracking a desired position for water monitoring missions. The vehicle self-steering system (autopilot system) is designed theoretically and tested via a simulation. Based on the Lyapunov theory, the stability in the closed-loop system is guaranteed, and the convergence of the heading tracking errors is obtained. In addition, the designed control law is implemented via a microcontroller and tested experimentally in real time. Conclusion, experimental results were carried out to verify the robustness of the designed controller when disturbances and uncertainties are introduced into the system.

**Keywords** Unmanned surface vehicle; Autopilot system design; Control law tuning; Heading controller; Backstepping integral control

## 1 Introduction

In the past decade, physicists have developed several mathematical models for studying wind (Bazionis and Georgilakis, 2021; Feijóo and Villanueva, 2016) and wave (Jeng et al., 2013) dynamics that have a considerable impact on the dynamics of sailing boats (Abrougui and Nejim, 2018).

Although environmental-force models are still insufficient to simulate the real behavior of the marine environment, these models can help researchers to understand and analyze the behavior of vessels and to design autopilot systems. Hence, Fossen made an assumption using the superposition of wind and wave disturbances (Fossen, 2011). Within the same framework, the authors of a previous study (Hu and Juang, 2011) designed a robust nonlinear course-keeping control method to control an unmanned

surface vehicle (USV) under the influence of high wind forces and large wave disturbances.

Generally, the effects of disturbing elements such as wind and waves must be considered when designing autopilot systems. The latter requires either data from many sensors, such as wind vanes, anemometers, and speedometers, or the estimation of some parameters, such as ocean current speed and direction, to enhance tracking accuracy.

The proportional integral derivative (PID) control technique (Caccia et al., 2008; Song et al., 2022; Park et al., 2010; Qi et al., 2007) represents the first implemented control algorithm in autopilot system designs. Most self-steering systems were designed using PID control method (Wang and Ackermann, 1998). Several course-keeping control techniques have also been presented in previous studies, including the fuzzy control technique (Hearn et al., 1997), adaptive control based on gain scheduling (Liu et al., 2017), neural network method (Ma et al., 2019), model predictive control (Siramdasu and Fahimi, 2012; Sharma et al., 2013; Bai et al., 2022), intelligent control using the genetic algorithm (Zhang et al., 2019), local control network approach (Sharma et al., 2012) and linear quadratic Gaussian control method (Asfihani et al., 2019).

Advanced control approaches, such as feedback linearization techniques (Phanthong et al., 2014; Winursito et al., 2022) and sliding mode control (Abrougui et al., 2021; Chen et al., 2019; Ashrafiuon et al., 2008; Gonzalez-Garcia and Castañeda, 2021), were designed to improve the system robustness with respect to modeling uncertainties.

## Article Highlights

- Nonlinear heading controller design using backstepping integral technique.
- Controller tuning.
- Autopilot system design for self-steering an Unmanned Surface Vehicle for waypoint tracking.

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In this study, we propose the design of an autopilot system based on the backstepping integral technique used for waypoint tracking. The heading controller was designed on the basis of external forces generated by ocean currents. The autopilot system demonstrated good performance during waypoint tracking in simulation and sea trials.

The remainder of this paper is structured as follows: The development of the mathematical model of the considered vehicle is presented in the second section. The heading controller, based on the backstepping integral method, is presented in the third section. The main contribution of this work is the tune of the developed heading controller.

The last section of this study addresses the design of a microcontroller-based autopilot system. Experimental results were presented to validate the developed control approach.

## 2 System modeling

### 2.1 Reference systems and vehicle description

The considered USV is presented in Figures 1 and 2. Figure 3 shows that the inertial reference frame  $R_0$  is  $(O, X_0, Y_0, Z_0)$  and the body fixed frame  $R$  is  $(G, X, Y, Z)$ . The origin of the body frame  $R$  is assumed to coincide with the USV's center of gravity as shown in Figure 3.



Figure 1 Unmanned surface vehicle used herein

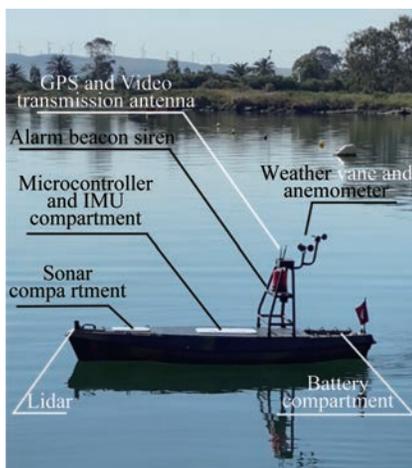


Figure 2 Hardware architecture of the USV

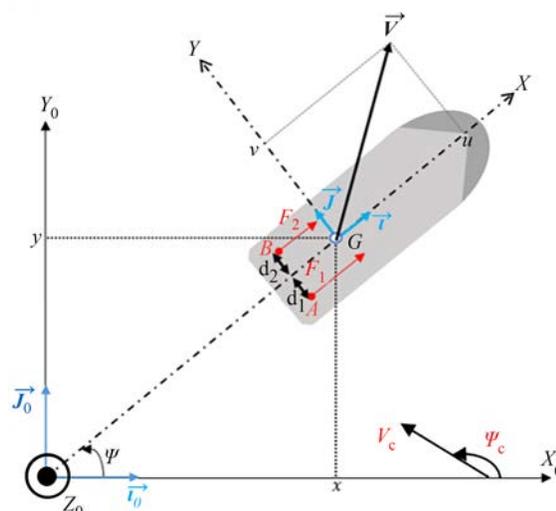


Figure 3 USV and reference systems

The USV actuator is composed of four electric motors, as illustrated in Figure 4.

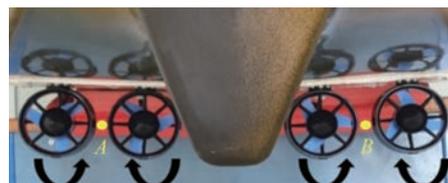


Figure 4 Rear view of thrusters

Thrusters control the USV heading and speed simultaneously by generating propulsion forces  $F_1$  and  $F_2$  on points  $A$  and  $B$ , respectively.

### 2.2 Equations of motion

The mathematical model of the USV can be simplified by using the following assumptions:

- Only surge  $u$ , sway  $v$ , and yaw  $r$  motions are modeled.
- The added-mass coefficients are modeled as constants.

All the variables used herein are presented and described in Table 1.

Therefore, the USV velocity expressed in the body frame is expressed as  $\vartheta = [u \ v \ r]^T$ .

Let us define  $\eta = [x \ y \ \psi]^T$ . This parameter describes the USV position  $(x, y)$  and heading  $\psi$  in the inertial frame.

On the basis of Fossen's model (Fossen, 2011), the USV mathematical model (vectorial form) can be presented as follows:

$$\dot{\eta} = J(\eta)\vartheta \tag{1}$$

$$M_{RB}\dot{\vartheta} + M_A\dot{\vartheta}_r + C_{RB}\vartheta + C_A\vartheta_r + D = \tau_1 + \tau_2 \tag{2}$$

with

**Table 1** Variable description

Notation	Description
$u$	Surge velocity
$v$	Sway velocity
$r$	Yaw rate
$\psi$	Heading angle
$F_2$	Left thrust force applied in $A$
$F_1$	Right thrust force applied in $B$
$m$	USV mass
$I_z$	Inertial moment around the $GZ$ axis
$x, y$	USV position in the $R_0$ frame
$\psi_c$	Direction of the marine current
$V_c$	Speed of the marine current
$X_{\dot{u}}, Y_{\dot{v}}$	Added mass along the $GX, GY$ axes
$N_{\dot{r}}$	Added mass around the $GZ$ axes
$d = d_1 = d_2$	Distance between $A$ and $B$ horizontally
$J(\eta)$	Transformation matrix from the $R$ -frame to the fixed frame

$$J(\eta) = \begin{bmatrix} \cos \psi & -\sin \psi & 0 \\ \sin \psi & \cos \psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (3)$$

$M_{RB}$  and  $M_A$  are the rigid and added-mass matrices, respectively.

$$M_{RB} = \begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & I_z \end{bmatrix} \quad (4)$$

$$M_A = - \begin{bmatrix} X_{\dot{u}} & 0 & 0 \\ 0 & Y_{\dot{v}} & 0 \\ 0 & 0 & N_{\dot{r}} \end{bmatrix} \quad (5)$$

$\mathcal{G}_r = (u_r \ v_r \ r)^T$  is the boat velocity relative to the water, which is expressed as follows:

$$\begin{bmatrix} u_r \\ v_r \end{bmatrix} = \begin{bmatrix} u \\ v \end{bmatrix} - \begin{bmatrix} \cos \psi & \sin \psi \\ -\sin \psi & \cos \psi \end{bmatrix} \begin{bmatrix} V_c \cos \psi_c \\ V_c \sin \psi_c \end{bmatrix} \quad (6)$$

$C_{RB}$  and  $C_A$  are the rigid-body Coriolis-centripetal and added-mass Coriolis matrices, respectively.

$$C_{RB} = \begin{bmatrix} 0 & -mr & 0 \\ mr & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \quad (7)$$

$$C_A = \begin{bmatrix} 0 & 0 & Y_{\dot{v}}v_r \\ 0 & 0 & -X_{\dot{u}}u_r \\ -Y_{\dot{v}}v_r & X_{\dot{u}}u_r & 0 \end{bmatrix} \quad (8)$$

$D$  is hydrodynamic damping matrix.

$$D = \begin{bmatrix} g_1(u_r) & 0 & 0 \\ 0 & g_2(v_r) & 0 \\ 0 & 0 & g_3(r) \end{bmatrix} \quad (9)$$

where  $g_1(u_r) = \alpha_1 u_r^{\beta_1}$ : surge resistance model along the  $GX$  axis;  $g_2(v_r) = \alpha_2 v_r^{\beta_2}$ : sway resistance model along the  $GY$  axis;  $g_3(r) = \alpha_3 r^{\beta_3}$ : yaw resistance model around the  $GZ$  axis;  $\tau_1$  and  $\tau_2$  are respectively the thrust force and the yaw moment. They are given as follows:

$$\tau_1 = \begin{bmatrix} F_1 + F_2 \\ 0 \\ 0 \end{bmatrix} \quad (10)$$

$$\tau_2 = \begin{bmatrix} 0 \\ 0 \\ (F_2 - F_1)d \end{bmatrix} \quad (11)$$

By using property 8.1 in (Fossen, 2011),

$$M_{RB}\dot{\mathcal{G}} + C_{RB}\mathcal{G} = M_{RB}\dot{\mathcal{G}}_r + C_{RB}\mathcal{G}_r \quad (12)$$

Equation (2) becomes

$$(m - X_{\dot{u}})\dot{u}_r = \tau_1 + rv_r(m + Y_{\dot{v}}) - g_1(u_r) \quad (13)$$

$$(m - Y_{\dot{v}})\dot{v}_r = -ru_r(m + X_{\dot{u}}) - g_2(v_r) \quad (14)$$

$$(I_z - N_{\dot{r}})\dot{r} = \tau_2 - u_rv_r(Y_{\dot{v}} - X_{\dot{u}}) - g_3(r) \quad (15)$$

Finally, a three degrees of freedom (3DOF) dynamic model of the USV is given as follows:

$$\left\{ \begin{array}{l} \dot{x} = u \cos \psi - v \sin \psi \\ \dot{y} = u \sin \psi + v \cos \psi \\ \dot{\psi} = r \\ \dot{u}_r = \frac{\tau_1 + rv_r(m + Y_{\dot{v}}) - g_1(u_r)}{m - X_{\dot{u}}} \\ \dot{v}_r = \frac{-ru_r(m + X_{\dot{u}}) - g_2(v_r)}{m - Y_{\dot{v}}} \\ \dot{r} = \frac{\tau_2 - (Y_{\dot{v}} - X_{\dot{u}})u_rv_r - g_3(r)}{I_z - N_{\dot{r}}} \\ u = u_r + V_c \cos(\psi - \psi_c) \\ v = v_r - V_c \sin(\psi - \psi_c) \end{array} \right. \quad (16)$$

The mathematical model (16) is highly nonlinear and has the form of  $\dot{X} = f(X, U)$ , where  $X = (x \ y \ \psi \ u_r \ v_r \ r)^T$  is the state vector, and  $U = (\tau_1 \ \tau_2)^T$  is the input control vec-

tor. Hydrodynamic coefficients were identified as described in a previous study (Abrougui et al., 2021). As discussed in the following section, a heading controller was designed and tested via simulation when the vehicle had to track desired waypoints.

### 3 Control system design

**Theorem 1** An autonomous system  $\dot{x} = f(x)$  has an equilibrium point  $x_e = 0$ , which is globally and asymptotically stable if a continuous scalar function  $V(x)$  with the following properties exists (Bacciotti and Rosier, 2005):

$$\begin{cases} V(0) = 0 \\ V(x) > 0 \quad \forall x \neq 0 \\ \lim_{x \rightarrow +\infty} V(x) = +\infty \\ \dot{V}(x) < 0 \quad \forall x \neq 0 \end{cases} \quad (17)$$

**Proof:** Let us consider a system written in the following form:

$$\begin{cases} \dot{x}_1 = f_1(x_1) + g_1(x_1)x_2 \\ \dot{x}_2 = f_2(x_1, x_2) + g_2(x_1, x_2)u(t) \end{cases} \quad (18)$$

where  $f$  and  $g$  are nonlinear functions, and  $u(t)$  is the input control.  $u(t)$  should be calculated by allowing  $x_1$  to converge to a setpoint  $x_{1d}$ .

First, let us define the error of the first variable  $x_1$  as

$$e_1 = x_{1d} - x_1 \quad (19)$$

Its time derivative is

$$\dot{e}_1 = \dot{x}_{1d} - \dot{x}_1 = \dot{x}_{1d} - f_1(x_1) - g_1(x_1)x_2 \quad (20)$$

Let us define the Lyapunov candidate function as follows:

$$V_1 = \frac{1}{2}e_1^2 + \frac{\beta_1}{2}\sigma^2 \quad (21)$$

with  $\sigma = e_1$ , and  $\beta_1$  is a positive design parameter.

The time derivative of  $V_1$  is

$$\begin{aligned} \dot{V}_1 &= e_1\dot{e}_1 + \beta_1\sigma\dot{\sigma} \\ &= e_1(\dot{x}_{1d} - f_1(x_1) - g_1(x_1)x_2 + \beta_1\sigma) \end{aligned} \quad (22)$$

The virtual control input  $x_2$  should be equal to  $x_{2d}$ , as given in the following equation. Letting  $\dot{V}(x) < 0$ :

$$x_{2d} = \frac{1}{g_1(x_1)}(k_1e_1 - f_1(x_1) + \dot{x}_{1d} + \beta_1\sigma) \quad (23)$$

where  $k_1 > 0$  is a design parameter, and  $g_1(x_1) \neq 0$ .

By substituting Equation (23) into (22), we obtain

$$\dot{V}_1 = -k_1e_1^2 < 0 \quad (24)$$

Second, let us define the error of the second variable as

$$e_2 = x_{2d} - x_2 \quad (25)$$

The time derivative of  $e_2$  is given by

$$\dot{e}_2 = \dot{x}_{2d} - \dot{x}_2 = \dot{x}_{2d} - f_2(x_1, x_2) - g_2(x_1, x_2)u(t) \quad (26)$$

Let us define the Lyapunov candidate function as follows:

$$V_2 = V_1 + \frac{1}{2}e_2^2 \quad (27)$$

Its time derivative is given by

$$\begin{aligned} \dot{V}_2 &= \dot{V}_1 + e_2\dot{e}_2 \\ &= e_1\dot{e}_1 + \beta_1\sigma e_1 + e_2(\dot{x}_{2d} - f_2(x_1, x_2) - g_2(x_1, x_2)u(t)) \end{aligned} \quad (28)$$

In the case of  $x_2 \neq x_{2d}$ , we have,

$$\begin{aligned} \dot{e}_1 &= \dot{x}_{1d} - \dot{x}_1 \\ &= \dot{x}_{1d} - f_1(x_1) - g_1(x_1)x_2 \\ &= \dot{x}_{1d} - f_1(x_1) - g_1(x_1)(x_{2d} - e_2) \\ &= \dot{x}_{1d} - f_1(x_1) + g_1(x_1)e_2 - k_1e_1 + f_1(x_1) - \dot{x}_{1d} - \beta_1\sigma \\ &= g_1(x_1)e_2 - k_1e_1 - \beta_1\sigma \end{aligned} \quad (29)$$

Equation (28) becomes

$$\begin{aligned} \dot{V}_2 &= e_1[g_1(x_1)e_2 - k_1e_1 - \beta_1\sigma] + \beta_1\sigma e_1 \\ &\quad + e_2[\dot{x}_{2d} - f_2(x_1, x_2) - g_2(x_1, x_2)u(t)] \\ &= g_1(x_1)e_2e_1 - k_1e_1^2 \\ &\quad + e_2[\dot{x}_{2d} - f_2(x_1, x_2) - g_2(x_1, x_2)u(t)] \end{aligned} \quad (30)$$

The input control  $u(t)$  should be expressed as follows to obtain  $\dot{V}_2 < 0$ .

$$u = \frac{1}{g_2(x_1, x_2)}(k_2e_2 - f_2(x_1, x_2) + \dot{x}_{2d} + g_1(x_1)e_1) \quad (31)$$

where  $k_2 > 0$  is a design parameter, and  $g_2(x_1, x_2) \neq 0$ . Let pose  $g_1(x_1) = g_1$ . The time derivative of Equation (23) is given by

$$\dot{x}_{2d} = \frac{1}{g_1}(k_1\dot{e}_1 - \dot{f}_1(x_1) + \ddot{x}_{1d} + \beta_1\dot{\sigma}) \quad (32)$$

By substituting Equation (32) into (30), we obtain

$$\dot{V}_2 = -k_1 e_1^2 - k_2 e_2^2 < 0 \tag{33}$$

Hence, the Lyapunov candidate function (27) decreases gradually, indicating that  $(e_1, \dot{e}_1)$  converge to 0 as  $t \rightarrow +\infty$ . Therefore, stability in the closed-loop system is established.

### 3.1 Heading controller design

From (16), we can extract the USV yaw dynamics as follows:

$$\begin{cases} \dot{\psi} = r \\ \dot{r} = \frac{\tau_2 - (Y_{\dot{v}} - X_{\dot{u}})u_r v_r - g_3(r)}{I_z - N_{\dot{r}}} \end{cases} \tag{34}$$

First, let us define the heading error  $e_1$  as  $e_1 = \psi_d - \psi$ . Its time derivative is

$$\dot{e}_1 = \dot{\psi}_d - r \tag{35}$$

Let us define the following Lyapunov candidate function as

$$V_1 = \frac{1}{2} e_1^2 + \frac{\beta}{2} \sigma^2 \tag{36}$$

with  $\dot{\sigma} = e_1$ .

The time derivative of  $V_1$  is

$$\dot{V}_1 = e_1 \dot{e}_1 + \beta \sigma e_1 = e_1 (\beta \sigma + \dot{\psi}_d - r) \tag{37}$$

From Equation (37), variable  $r$  should converge to  $r_d$  to ensure  $\dot{V}_1 < 0$ .

$$r_d = k_1 e_1 + \beta \sigma + \dot{\psi}_d \tag{38}$$

Using Equations (37) and (38), we obtain

$$\dot{V}_1 = -k_1 e_1^2 < 0 \tag{39}$$

where  $k_1 > 0$  is a design control parameter.

Second, let us define the error  $e_2$  of the variable  $r$  as

$$e_2 = r_d - r \tag{40}$$

Its time derivative is expressed as

$$\dot{e}_2 = \dot{r}_d - \dot{r} \tag{41}$$

Let us define the following Lyapunov candidate function as follows:

$$V_2 = V_1 + \frac{1}{2} e_2^2 \tag{42}$$

Its time derivative is given by

$$\begin{aligned} \dot{V}_2 &= \dot{V}_1 + e_2 \dot{e}_2 \\ &= e_1 \dot{e}_1 + \beta \sigma e_1 + e_2 \dot{e}_2 \\ &= e_1 (\dot{\psi}_d - r) + \beta \sigma e_1 + e_2 \dot{e}_2 \\ &= e_1 (\dot{\psi}_d - (r_d - e_2)) + \beta \sigma e_1 + e_2 (\dot{r}_d - \dot{r}) \end{aligned} \tag{43}$$

where  $r_d = k_1 e_1 + \beta \sigma + \dot{\psi}_d$ . Therefore, we obtain

$$\dot{V}_2 = e_1 (e_2 - k_1 e_1) + e_2 (\dot{r}_d - \dot{r}) \tag{44}$$

The angular acceleration  $\dot{r}$  is chosen as follows to verify  $\dot{V}_2 < 0$ :

$$\dot{r} = k_2 e_2 + e_1 + \dot{r}_d \tag{45}$$

where  $k_2 > 0$  is a design control parameter and

$$\dot{r}_d = k_1 \dot{e}_1 + \beta e_1 + \ddot{\psi}_d \tag{46}$$

Using (44) and (45), we acquire

$$\dot{V}_2 = -k_1 e_1^2 - k_2 e_2^2 < 0 \quad \forall (e_1, e_2) \neq (0, 0) \tag{47}$$

Therefore, using (34) and (45), the heading controller  $\tau_2$  is expressed as follows:

$$\begin{aligned} \tau_2 &= (I_z - N_{\dot{r}})(k_2 e_2 + e_1 + \dot{r}_d) + (Y_{\dot{v}} - X_{\dot{u}})u_r v_r + g_3(r) \\ &= (I_z - N_{\dot{r}})(e_1(1 + \beta + k_1 k_2) - r(k_2 + k_1) - \beta \sigma k_2) + \\ &\quad (Y_{\dot{v}} - X_{\dot{u}})u_r v_r + g_3(r) \end{aligned} \tag{48}$$

with

$$\begin{aligned} u_r &= u - V_C \cos(\psi - \psi_C) \\ v_r &= v + V_C \sin(\psi - \psi_C) \end{aligned}$$

The parameters  $k_1$ ,  $k_2$ , and  $\beta$  that remain to be determined are as follows:

From Equation (38), we have

$$\dot{\psi}_d = r_d - k_1 e_1 - \beta \sigma \tag{49}$$

Therefore, Equation (35) becomes

$$\begin{aligned} \dot{e}_1 &= \dot{\psi}_d - r \\ &= r_d - k_1 e_1 - \beta \sigma - r \\ &= (r_d - r) - k_1 e_1 - \beta \sigma \\ &= e_2 - k_1 e_1 - \beta \sigma \end{aligned} \tag{50}$$

Using Equations (41) and (45), we obtain

$$\dot{e}_2 = -k_2 e_2 - e_1 \tag{51}$$

Consequently, we have

$$\begin{cases} \dot{e}_1 = e_2 - k_1 e_1 - \beta \sigma \\ \dot{e}_2 = -k_2 e_2 - e_1 \\ \dot{\sigma} = e_1 \end{cases} \tag{52}$$

Therefore, we have

$$\begin{bmatrix} \dot{e}_1 \\ \dot{e}_2 \\ \dot{\sigma} \end{bmatrix} = \begin{bmatrix} -k_1 & 1 & -\beta \\ -1 & -k_2 & 0 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} e_1 \\ e_2 \\ \sigma \end{bmatrix} \tag{53}$$

The characteristic polynomial is

$$P(s) = \begin{vmatrix} s + k_1 & -1 & \beta \\ 1 & s + k_2 & 0 \\ -1 & 0 & s \end{vmatrix} = s^3 + (k_1 + k_2)s^2 + (k_1 k_2 + \beta + 1)s + k_2 \beta \tag{54}$$

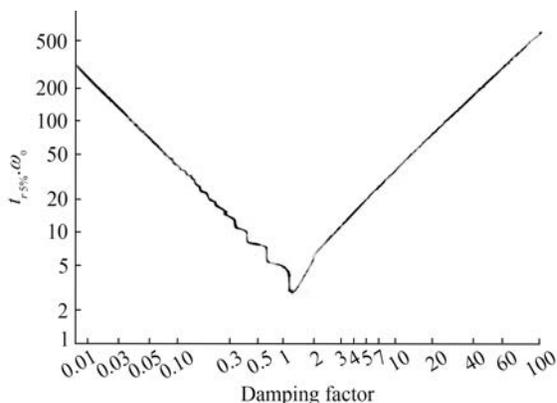
It has the following form:

$$P(s) = (s - s_0)(s - s_1)(s - s_2) \tag{55}$$

where  $s_0, s_1, s_2$  are designed as three poles allowing the heading dynamic to behave as desired.

$(s - s_1)(s - s_2)$  can be seen as a second-order polynomial with  $s_1 = s_2$ . It can be written in the form of  $s^2 + 2\zeta\omega s + \omega^2$ , where  $\zeta = 1$  is the damping ratio, and  $\omega$  is the undamped natural frequency.

If we want to force the third-order system (55) to behave like a second-order system, we have to choose  $|s_0| \gg |s_1|$  as  $\zeta = 1$ . According to Figure 5,  $\omega = \frac{5}{t_{r,5\%}}$ , where  $t_{r,5\%}$  is the desired 5% response time.



**Figure 5** Response time of the second-order system as function of the damping ratio

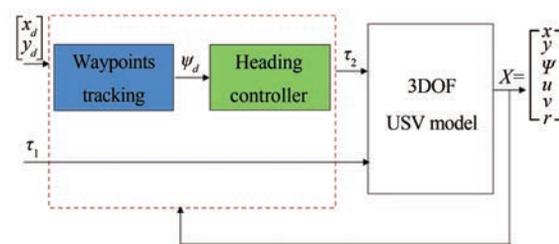
Let us select  $|s_0| = 20|s_1|$  to obtain  $|s_0| \gg |s_1|$ . By developing the polynomial  $(s + 20\omega)(s + \omega)^2$  and using (55), we obtain

$$\begin{cases} k_1 + k_2 = 22\omega \\ k_1 k_2 + \beta + 1 = 41\omega^2 \\ k_2 \beta = 20\omega^3 \end{cases} \tag{56}$$

By choosing  $t_{r,5\%} = 3s$ , we obtain  $k_1 = 3.3$  and  $k_2 = 33.37$  at  $\beta = 2.775$ .

### 3.2 High-level controller design

Guidance is a system that generates the desired heading  $\psi_d$  to be used as input into the heading controller (Figure 6).



**Figure 6** Autopilot scheme

The desired heading  $\psi_d$  can be given by

$$\psi_d = \tan^{-1} \left( \frac{y - y_d}{x - x_d} \right) \tag{57}$$

$(x, y)$  is the actual position of the USV, and  $(x_d, y_d)$  the desired position of the USV.  $\psi_d$  represents the direction to the target position (line of sight).

$\tau_1$  is chosen constant and equal to 50% of the total thrust force during the simulation and experimental tests.

## 4 Simulation and experimental results

### 4.1 Simulation results

A simulation test was conducted to test the performance of the proposed method for tuning the heading controller. In this context, we introduced three target positions into the guidance system.

The ocean current velocity and direction were set to ( $V_c = 0.1$  m/s,  $\psi_c = -90^\circ$ ), and the used normalized parameters (Abrougui et al., 2021) are given in Table 2.

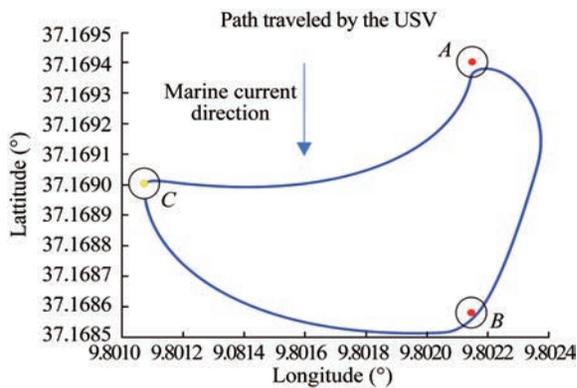
The path of the USV is shown in Figure 7. The desired waypoints were well reached by the USV despite the presence of model uncertainties and disturbances owing to the ocean current.

The time evolution of the USV heading, as illustrated in

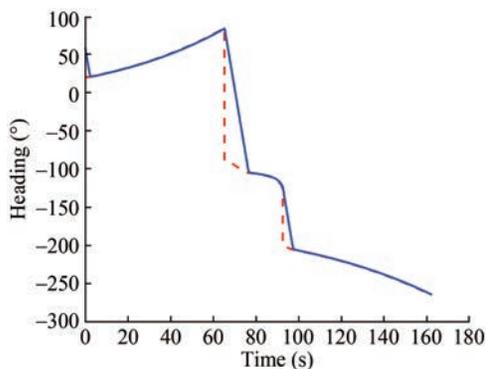
Figure 8, shows that the system responded rapidly, accurately, and without overshooting during the steady state as desired.

**Table 2** Evaluation of Parameters

Notation	Value
$X_u$ (kg/N)	$4.5 \times 10^{-4}$
$Y_v$ (kg/N)	$1.8 \times 10^{-3}$
$N_r$ (kg·m <sup>2</sup> /N)	$2.16 \times 10^{-2}$
$m$ (kg/N)	0.009
$I_z$ (kg·m <sup>2</sup> /N)	$6 \times 10^{-2}$
$d$ (m)	0.24
$\alpha_1$	0.329 9
$\beta_1$	1.646 6
$\alpha_2$	4
$\beta_2$	1
$\alpha_0$	0.24
$\alpha_3$	0.85
$\beta_3$	1

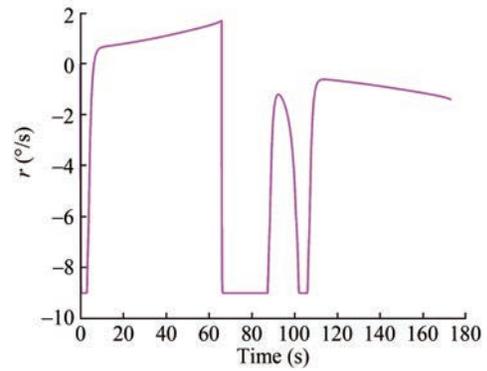


**Figure 7** Path followed by the USV during the simulation

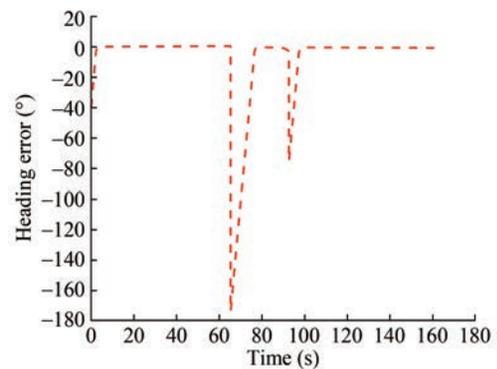


**Figure 8** Time evolution of the USV heading

Figure 9 presents the evolution of the yaw rate. The yaw rate was constantly equal to zero unless the USV heading changed.



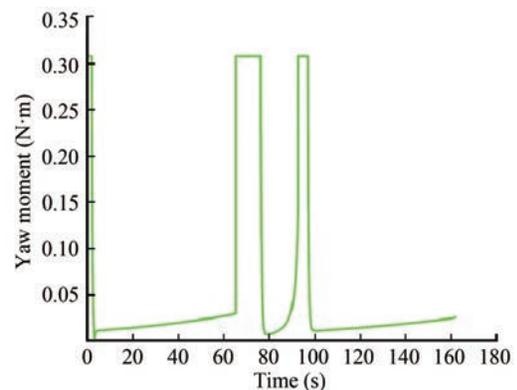
**Figure 9** Yaw rate



**Figure 10** Time evolution of the heading error  $e_1(t)$

Figure 10 shows that the heading error is always zero as demonstrated in section 3. Consequently, the effectiveness of the proposed method in terms of the accuracy of the designed controller was proven.

The controller  $\tau_2$  (Figure 11) is capable of providing control action to minimize the error in heading. Figure 12 shows also that the generated control inputs for left and right thrusts were smooth. Moreover, no chattering problem was observed. These satisfactory tracking performances clearly demonstrate the efficiency of the heading controller tuning approach.



**Figure 11** Yaw moment

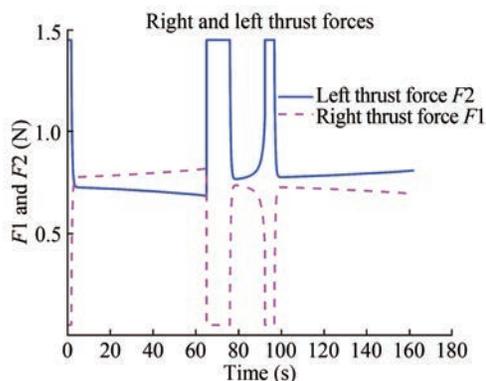


Figure 12 Yaw moment

### 4.2 Experimental results

As discussed in this section, an ATmega2560 microcontroller was used to implement the developed autopilot approach (see the hardware architecture of the autopilot system described in Figure 13). The designed heading controller (Equation (48)) was implemented via the Arduino integrated development environment. The parameters  $k_1$ ,  $k_2$ , and  $\beta$  were calculated as described in Section 3.1.



Figure 13 Proposed autopilot system hardware

Figure 12 presents the system hardware, which comprises

- an inertial measurement unit (MPU 9250 with its library from GitHub),
- a GPS (NEO 7M) for measuring the USV position and speed on the ground;
- a SD card reader for data logging.

As shown in Figures 14 and 15, the USV reached all the waypoints 1, 2, and 3, even in the presence of environmental disturbances due to ocean currents.

In contrast to the simulation result presented in Figure 9,

the experimental results in Figures 17 and 18 illustrate that the USV heading converged to the desired heading with some fluctuations, which occurred owing to the noisy measurements originating from the compass sensor.

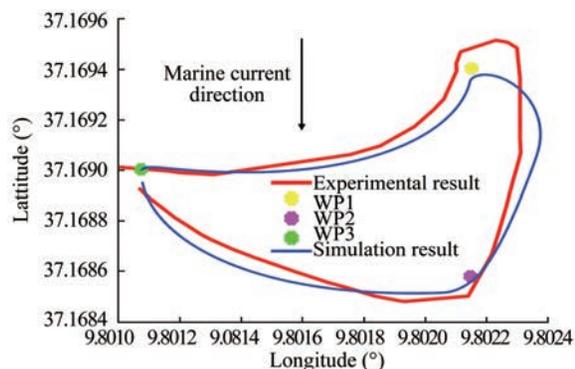


Figure 14 Paths followed by the USV during the simulation and experimental tests

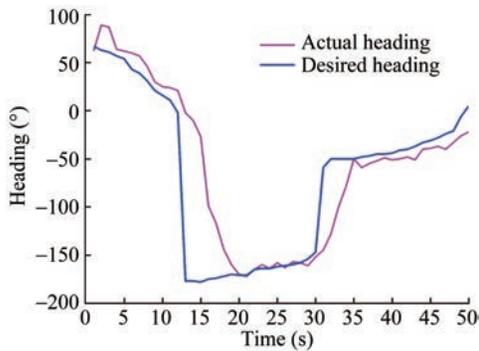


Figure 15 Path followed by the USV during the experimental test

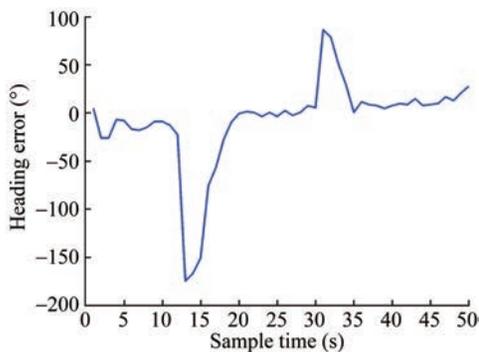


Figure 16 USV whenreaching waypoints

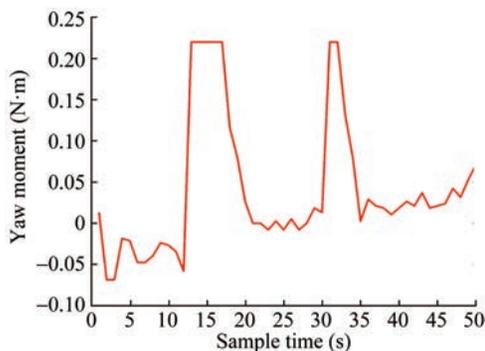
Figure 19 shows the time evolution of the designed controller  $\tau_2$  (yaw moment) during the experimental test letting the USV heading to track desired ones in order to reach all the given waypoints successively. The calculated yaw moment was converted into a pulse-width modulation PWM signal for controlling the differential thrust force via a microcontroller.



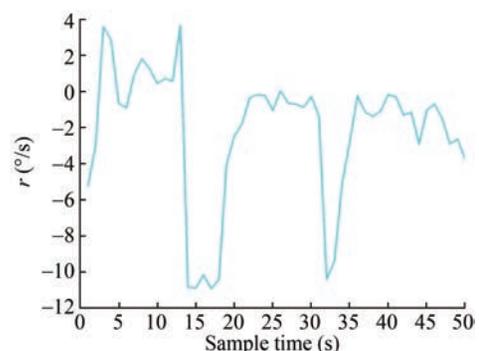
**Figure 17** Time evolution of the desired and actual heading during the experimental test (sample time is 35 ms)



**Figure 18** Time evolution of the heading error during the experimental test (sample time is 35 ms)



**Figure 19** Time evolution of the input control during the experimental test (sample time is 35 ms)



**Figure 20** Time evolution of the yaw rate during the experimental test (sample time is 35 ms)

## 5 Conclusions

This study addressed the design of an autopilot system for controlling a USV. In a previous study (Abrougui et al., 2021), the sliding mode control was applied, evaluated, and tested in real time for controlling the USV. In this study, another technique was used to develop an autopilot system based on the backstepping integral method. The control stability of the developed system was proven based on Lyapunov theory. An approach for tuning the heading controller was also proposed and tested. Simulation and experimental results were presented to demonstrate the effectiveness of the proposed control law. The next work will be conducted to add an obstacle avoidance system to the proposed autopilot.

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## References

- Abrougui H, Nejim S (2018) Backstepping control of an autonomous catamaran sailboat. *Robotic Sailing*, 41-50
- Abrougui H, Nejim S, Hachicha S, Zaoui C, Dallagi H (2021) Modeling, parameter identification, guidance and control of an unmanned surface vehicle with experimental results. *Ocean Engineering*, 241, 110038
- Asfihani T, Arif DK, Putra FP, Firmansyah MA (2019) Comparison of LQG and adaptive PID Controller for USV heading control. *Journal of Physics: Conference Series* 1218(1): 012058
- Ashrafioun H, Muske KR, McNinch LC, Soltan RA (2008) Sliding-mode tracking control of surface vessels. *IEEE Transactions on Industrial Electronics* 55(11): 4004-4012
- Bacciotti A, Rosier L (2005) *Lyapunov functions and stability in control theory*. Springer Science & Business Media
- Bai X, Li B, Xu X, Xiao Y (2022) A review of current research and advances in unmanned surface vehicles. *Journal of Marine Science and Application* 21(2): 47-58
- Bazonis IK, Georgilakis PS (2021) Review of deterministic and probabilistic wind power forecasting: Models, methods, and future research. *Electricity* 2(1): 13-47
- Caccia M, Bibuli M, Bono R, Bruzzone G (2008) Basic navigation, guidance and control of an unmanned surface vehicle. *Autonomous Robots* 25(4): 349-365
- Chen Z, Zhang Y, Zhang Y, Nie Y, Tang J, Zhu S (2019) Disturbance-observer-based sliding mode control design for nonlinear unmanned surface vessel with uncertainties. *IEEE Access* 7: 148522-148530
- Feijóo A, Villanueva D (2016) Assessing wind speed simulation methods. *Renewable and Sustainable Energy Reviews* 56: 473-483
- Fossen TI (2011) *Handbook of marine craft hydrodynamics and motion control*. John Wiley & Sons
- Gonzalez-Garcia A, Castañeda H (2021) Guidance and control based on adaptive sliding mode strategy for a USV subject to uncertainties. *IEEE Journal of Oceanic Engineering* 46(4): 1144-1154
- Hearn GE, Zhang Y, Sen P (1997) Alternative designs of neural

- network-based autopilots: a comparative study. *IFAC Proceedings Volumes* 30(22): 83-88
- Hu SS, Juang JY (2011) Robust nonlinear ship course-keeping control under the influence of high wind and large wave disturbances. *8th Asian Control Conference*, 393-398
- Jeng DS, Ye JH, Zhang JS, Liu PF (2013) An integrated model for the wave-induced seabed response around marine structures: Model verifications and applications. *Coastal Engineering* 72: 1-19
- Liu L, Wang D, Peng Z, Li T (2017) Modular adaptive control for LOS-based cooperative path maneuvering of multiple underactuated autonomous surface vehicles. *IEEE Transactions on Systems, Man, and Cybernetics: Systems* 47(7): 1613-1624
- Ma LY, Xie W, Huang HB (2019) Convolutional neural network-based obstacle detection for unmanned surface vehicle. *Mathematical Biosciences and Engineering* 17(1): 845-861
- Park JH, Shim HW, Jun BH, Kim SM, Lee PM, Lim YK (2010) A model estimation and multi-variable control of an unmanned surface vehicle with two fixed thrusters. *Oceans'10, Sydney*, 1-5
- Phanthong T, Maki T, Ura T, Sakamaki T, Aiyarak P (2014) Application of A\* algorithm for real-time path re-planning of an unmanned surface vehicle avoiding underwater obstacles. *Journal of Marine Science and Application* 13(1): 105-116
- Qi J, Peng Y, Wang H, Han J (2007) Design and implement of a trimaran unmanned surface vehicle system. *2007 International Conference on Information Acquisition*, 361-365
- Sharma SK, Naeem W, Sutton R (2012) An autopilot based on a local control network design for an unmanned surface vehicle. *J. Navigation* 65(2): 281-301. DOI: 10.1017/S0373463311000701
- Sharma SK, Sutton R, Motwani A, Annamalai A (2013) Non-linear control algorithms for an unmanned surface vehicle. *Proceedings of the Institution of Mechanical Engineers, Part M, Journal of Engineering for the Maritime Environment* 227(4): 1-10
- Siramdasu Y, Fahimi F (2012) Incorporating input saturation for underactuated surface vessel trajectory tracking control. *American Control Conference, Montreal*, 6203-6208
- Song L, Xu C, Hao L, Yao J, Guo R (2022) Research on PID parameter tuning and optimization based on SAC-Auto for USV path following. *Journal of Marine Science and Engineering* 10(12): 1847
- Wang L, Ackermann J (1998) Robustly stabilizing PID controllers for car steering systems. *Proceedings of the 1998 American Control Conference, Philadelphia*, 1, 41-42. DOI: 10.1109/ACC.1998.694624
- Winursito A, Dhewa OA, Nasuha A, Pratama GN (2022) Integral state feedback controller with coefficient diagram method for USV heading control. *5th International Conference on Information and Communications Technology*, 295-300
- Zhang W, Xu Y, Xie J (2019) Path planning of USV based on improved hybrid genetic algorithm. *European Navigation Conference, Warsaw*, 1-7. DOI: 10.1109/EURONAV.2019.8714160